



# Kinetics of ammonia consumption during the selective catalytic reduction of NO<sub>x</sub> over an iron zeolite catalyst

V. Bacher<sup>a</sup>, C. Perbandt<sup>b</sup>, M. Schwefer<sup>b</sup>, R. Siefert<sup>b</sup>, S. Pinnow<sup>b</sup>, T. Turek<sup>a,\*</sup>

<sup>a</sup> Institute of Chemical Process Engineering, Clausthal University of Technology, 38678 Clausthal-Zellerfeld, Germany

<sup>b</sup> ThyssenKrupp Industrial Solutions AG, 44141 Dortmund, Germany

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## ABSTRACT

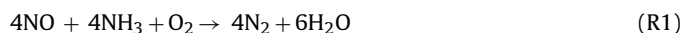
The steady-state kinetics of the selective catalytic reduction (SCR) of nitrogen oxides (NO and NO<sub>2</sub>) with ammonia over a commercial iron zeolite catalyst were studied in the temperature range of 250 to 450 °C using an integral tubular reactor. Special attention was paid to the stoichiometric ratio of the conversion of ammonia and nitrogen oxides. For this purpose, both systematic SCR measurements at different feed gas compositions and independent studies of the catalytic oxidation of ammonia in the absence of NO and NO<sub>2</sub> were carried out. Under all reaction conditions, a considerable deviation from the expected 1:1 stoichiometry was observed. The steady-state kinetics of the reacting system could be described by global Langmuir–Hinshelwood-type rate equations for *standard* SCR, *fast* SCR, NO/NO<sub>2</sub> equilibrium and NH<sub>3</sub> oxidation. For the correct calculation of the ammonia oxidation it was necessary to include two terms. A first one describing the reaction of NH<sub>3</sub> with O<sub>2</sub>, which becomes important at temperatures above 400 °C, and a second rate equation which is not only proportional to NH<sub>3</sub> and O<sub>2</sub> but also to the NO concentration and which is of particular relevance at low reaction temperatures. Additional measurements with different catalyst particle sizes including industrial extrudates could be successfully described with the aid of a reactor model which took film and pore diffusion phenomena into account.

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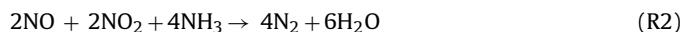
## 1. Introduction

Iron exchanged zeolites are highly efficient catalysts for the reduction of NO<sub>x</sub> (NO and NO<sub>2</sub>) with ammonia. As non-toxic materials with similarly high nitrogen oxides reduction activity as the classical vanadia–titania catalyst, iron zeolites are now being widely used for the removal of NO<sub>x</sub> from automotive exhaust streams [1]. In addition to NO<sub>x</sub> removal, iron zeolites are also capable of decomposing or reducing N<sub>2</sub>O very efficiently. Based on these unique properties, the EnviNOx<sup>®</sup> process for the combined catalytic destruction of all types of nitrogen oxide present in nitric acid tail gases has been developed [2]. Proper design of processes for automotive and stationary removal of nitrogen oxides necessitates the development of kinetic models for the exact calculation of the nitrogen oxide removal rates and the corresponding required

amount of the reducing agent ammonia. It is generally accepted that several stoichiometric equations must be considered for successful description of the kinetics of the selective catalytic reaction (SCR) of nitrogen oxides. Nitric oxide reacts with oxygen and ammonia according to the so-called *standard* SCR reaction:



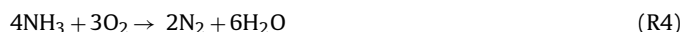
while in the presence of nitrogen dioxide the *fast* SCR (R2) with a much higher reaction rate prevails.



Even in the absence of NO<sub>2</sub> in the exhaust gas, the *fast* SCR must be taken into account since iron zeolites exhibit a certain catalytic activity for the equilibrium reaction between NO and NO<sub>2</sub>:



If the NO<sub>2</sub>:NO<sub>x</sub> ratio is below about 50%, the direct reaction of NO<sub>2</sub> with ammonia can be neglected due to the *fast* SCR proceeding much more rapidly [3]. Furthermore, the reducing agent ammonia undergoes catalytic oxidation towards N<sub>2</sub> in the presence of O<sub>2</sub>, especially at higher reaction temperatures:



\* Corresponding author. Tel.: +49 5323 722184; fax: +49 5323 722182.

E-mail addresses: [bacher@icvt.tu-clausthal.de](mailto:bacher@icvt.tu-clausthal.de) (V. Bacher),

[christian.perbandt@thyssenkrupp.com](mailto:christian.perbandt@thyssenkrupp.com) (C. Perbandt),

[meinhard.schwefer@thyssenkrupp.com](mailto:meinhard.schwefer@thyssenkrupp.com) (M. Schwefer),

[rolf.siefert@thyssenkrupp.com](mailto:rolf.siefert@thyssenkrupp.com) (R. Siefert), [stefan.pinnow@thyssenkrupp.com](mailto:stefan.pinnow@thyssenkrupp.com)

(S. Pinnow), [turck@icvt.tu-clausthal.de](mailto:turck@icvt.tu-clausthal.de) (T. Turek).

## Nomenclature

$a$	volume specific geometric catalyst surface area ( $\text{m}^{-1}$ )
$c_{G,i}$	gas-phase concentration of species $i$ ( $\text{mol}/\text{m}^3$ )
$c_{S,i}$	catalyst concentration of species $i$ ( $\text{mol}/\text{m}^3$ )
$D_{e,i}$	effective diffusivity of species $i$ ( $\text{m}^2/\text{s}$ )
$E_{A,j}$	activation energy of reaction $j$ ( $\text{J}/\text{mol}$ )
$k_{0,j}$	frequency factor of reaction $j$ (different)
$K_i$	adsorption constant for species $i$ (different)
$n_i$	reaction order for species $i$ (–)
$r_j$	rate of reaction $j$ ( $\text{mol}/(\text{kg s})$ )
$R_{\text{sph}}$	equivalent radius of catalyst particle (m)
$R$	ideal gas constant ( $8.3145 \text{ J}/(\text{mol K})$ )
$T$	temperature (K)
$u_{G,0}$	superficial gas velocity ( $\text{m}/\text{s}$ )
$x$	internal catalyst coordinate (m)
$z$	axial reactor coordinate (m)
$\beta_i$	mass transfer coefficient of species $i$ ( $\text{m}/\text{s}$ )
$\nu_{i,j}$	stoichiometric coefficient of species $i$ in reaction $j$ (–)
$\rho_{\text{cat}}$	apparent catalyst density ( $\text{kg}/\text{m}^3$ )

Several models have been developed to describe the kinetics of the catalytic reduction of nitrogen oxides over iron exchanged zeolites, both for steady-state and transient conditions. Extensive work by Tronconi and coworkers has shown that many features of the SCR kinetics on vanadia–titania catalysts can be transferred to iron zeolite catalysts [4–8]. It is generally accepted that ammonia adsorbs strongly under reaction conditions while different adsorbed nitrogen oxides species are discussed as reaction intermediates [3].

One of the remaining unresolved questions regarding the kinetics of SCR on iron zeolites is related to the stoichiometry of the reaction between ammonia and nitrogen oxides. Sachtler and coworkers [9] have raised the question of the SCR stoichiometry. These authors pointed out that the direct reaction of NO with  $\text{NH}_3$  would result in an  $\text{NH}_3$ :NO ratio of 0.66 according to



if NO is not oxidized to  $\text{NO}_2$  and  $\text{NH}_3$  does not react with  $\text{O}_2$ . On the other hand, if NO is rapidly oxidized and  $\text{NO}_2$  the sole oxidant, the following reaction with a stoichiometric ratio of 1.33 would be obtained:

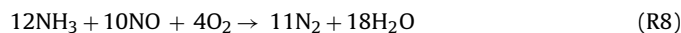


During their experimental investigations, these authors observed that a molar excess of 10 to 40% of  $\text{NH}_3$  was required to reduce a certain amount of  $\text{NO}_x$  [9]. Devadas et al. [10] have also shown that significant deviations from the postulated stoichiometry of 1:1 according to reactions (R1) and (R2) occur. These authors, and later also Wang et al. [11], suggested that the observed excess  $\text{NH}_3$  consumption is caused by the ammonia oxidation reaction (R4). However, Schuler et al. [12,13] demonstrated that this cannot be the only reason as the over-consumption of ammonia is more pronounced at lower temperatures where the relatively slow ammonia oxidation does not take place to a significant extent. Schuler et al. postulated that either a surface species might be formed during standard SCR which passes through a redox cycle consuming  $\text{NH}_3$  for reduction and  $\text{O}_2$  for oxidation [12] or that ammonia could be decomposed to the elements [13]. In these studies, the stoichiometric deviations were accounted for modeling purposes by empirical temperature-dependent factors. Markatou et al. [14] presented a kinetic model for SCR over iron

zeolite catalysts and incorporated the ammonia oxidation not only to nitrogen (R4) but also to nitric oxide:



Sjövall et al. [15] introduced, in addition to standard SCR (R1) and ammonia oxidation (R4), a further stoichiometric equation



which results in a constant additional ammonia demand of 20% for each mole of NO converted. Colombo et al. incorporated the concentration of NO as additional term in their kinetic expression for reaction (R4) [16]. This approach results in an acceleration of the ammonia oxidation whenever NO is present. Very recently, Olsson and coworkers presented mechanistic evidence – by careful studies with isotopically labeled reactants – that the parasitic oxidation of  $\text{NH}_3$  occurring at low temperatures is enhanced in the presence of NO [17]. These authors proposed that reaction (R7) yielding NO is mainly responsible for this effect, although the oxidation of ammonia to nitrogen according to reaction (R4) could not be ruled out.

In our contribution a refined approach for the description of the ammonia oxidation kinetics during the SCR of nitrogen oxides is presented. We introduce a second term in the ammonia oxidation rate equation which is not only dependent on the  $\text{NH}_3$  and  $\text{O}_2$  concentrations, but also a function of the NO content. This approach reflects an  $\text{NH}_3$  consuming redox cycle without reduction of NO as proposed by Schuler et al. [12]. Consequently, the activation energy of the additional reaction is allowed to differ from the value for the ammonia oxidation reaction with  $\text{O}_2$  in the absence of NO. Since the aim of the study is the description of steady-state catalyst operation, global Langmuir–Hinshelwood-type rate equations are used. It will be shown that this kinetic approach is capable of describing the  $\text{NH}_3$ : $\text{NO}_x$  stoichiometry with good accuracy over a broad range of temperatures and concentrations of NO,  $\text{NO}_2$ ,  $\text{NH}_3$  and  $\text{O}_2$ . Moreover, the influence of mass transfer resistances during measurements with different catalyst sieve fractions can also be successfully described.

## 2. Methods

### 2.1. Experimental

The experiments were carried out with a commercial iron zeolite catalyst (Clariant Produkte (Deutschland) GmbH, EnviCat®- $\text{NO}_x$ ). Details of the experimental method have been described elsewhere [18]. Briefly, catalyst extrudates that had been kept under working conditions in a nitric acid exhaust gas stream for three months were used as received or crushed and sieved to different fractions. The exact shape of the catalyst bodies is proprietary and cannot be disclosed. If not otherwise noted, the measurements were performed with 0.94 g of these fractions diluted with the same volume of glass beads or silicon carbide particles (315 to 500  $\mu\text{m}$ ) and loaded into a tubular stainless steel reactor (18 mm ID) that was coated with silica through a sol–gel method to prevent ammonia oxidation at the reactor wall. In blank tests with an uncoated stainless steel reactor it was found that considerable amounts of  $\text{NH}_3$  reacted above temperatures of 350 °C.

Reactant mixtures with a total flow rate of 2000  $\text{cm}^3/\text{min}$  (NTP) were obtained by feeding NO,  $\text{NO}_2$ ,  $\text{NH}_3$ ,  $\text{H}_2\text{O}$ ,  $\text{O}_2$  and  $\text{N}_2$  via mass flow controllers (Bronkhorst High-Tech) at an absolute reactor pressure of 1.7 bar which was maintained with a regulating valve (Bronkhorst High-Tech). Gas analysis of inlet and outlet reactor streams was carried out with an FTIR spectrometer (Nicolet 5700, Thermo Scientific) and an oxygen analyzer (Oxymat 6, Siemens). The reactions were studied at temperatures from 250 to 450 °C

with feeds containing 0 to 400 ppm NO, 0 to 125 ppm NO<sub>2</sub>, 104 to 962 ppm NH<sub>3</sub>, 1.2 to 4.0 vol% O<sub>2</sub> and 0.16 to 2.0 vol% H<sub>2</sub>O balanced in N<sub>2</sub>.

## 2.2. Kinetic analysis of measured data

The measured reactant concentrations at the reactor outlet were analyzed with a steady-state, heterogeneous 1D + 1D reactor model. Given the low heats of reaction in the diluted gas streams, isothermal reactor operation was assumed. The lengths of the catalytic packings were sufficiently high to ensure plug flow behavior at Bodenstein numbers (or reactor Peclet numbers) larger than 100 [19]. Pressure drop and density changes of the gas flow were neglected. The following mass balance equations and boundary conditions were used:

### • Gas phase

$$\text{Mass balance } u_{G,0} \frac{dc_{G,i}}{dz} = -\beta_i a(c_{G,i} - c_{S,i}) \quad (1)$$

$$\text{Boundary condition } (z = 0) \quad c_{G,i} = c_{G,i,0} \quad (2)$$

Here,  $u_{G,0}$  is the superficial gas velocity,  $z$  the axial reactor coordinate and  $a$  the average value of the specific geometric catalyst surface area assuming spherical geometry.  $c_{G,i}$  and  $c_{S,i}$  are the reactant concentrations in the gas phase and at the outer catalyst surface, respectively. The mass transfer coefficients  $\beta_i$  for packed beds were calculated from Sherwood numbers, which were determined in analogy to Nusselt numbers [20]. The required molecular diffusion coefficients were obtained from Massman [21].

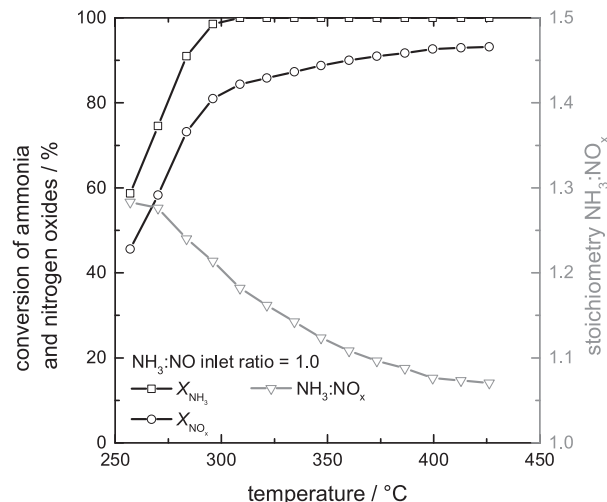
### • Catalyst phase

$$\text{Mass balance } D_{e,i} \frac{d^2 c_{S,i}}{dx^2} = -\rho_{\text{cat}} \sum_j v_{i,j} r_j \quad (3)$$

$$\text{Boundary condition } (x = 0) \quad \frac{dc_{S,i}}{dx} = 0 \quad (4)$$

$$\text{Boundary condition } (x = R_{\text{sph}}) \quad D_{e,i} \frac{dc_{S,i}}{dx} = \beta_i a(c_{G,i} - c_{S,i}) \quad (5)$$

Here,  $x$  is the internal catalyst coordinate,  $R_{\text{sph}}$  the equivalent radius of the catalyst particles,  $\rho_{\text{cat}}$  the apparent catalyst density,  $D_{e,i}$  the effective diffusivity and  $v_{i,j}$  the stoichiometric coefficient of species  $i$  in reaction  $j$ . Note that Eq. (3) is derived for slab geometry of



**Fig. 1.** NH<sub>3</sub> and NO conversions as well as stoichiometric ratio of converted NH<sub>3</sub> and NO<sub>x</sub> amounts as a function of temperature for an equimolar reactant mixture. 2.5 vol% O<sub>2</sub>, 400 ppm NO, 400 ppm NH<sub>3</sub> and 3100 ppm H<sub>2</sub>O at reactor inlet, catalyst sieve fraction 315–500  $\mu\text{m}$ .

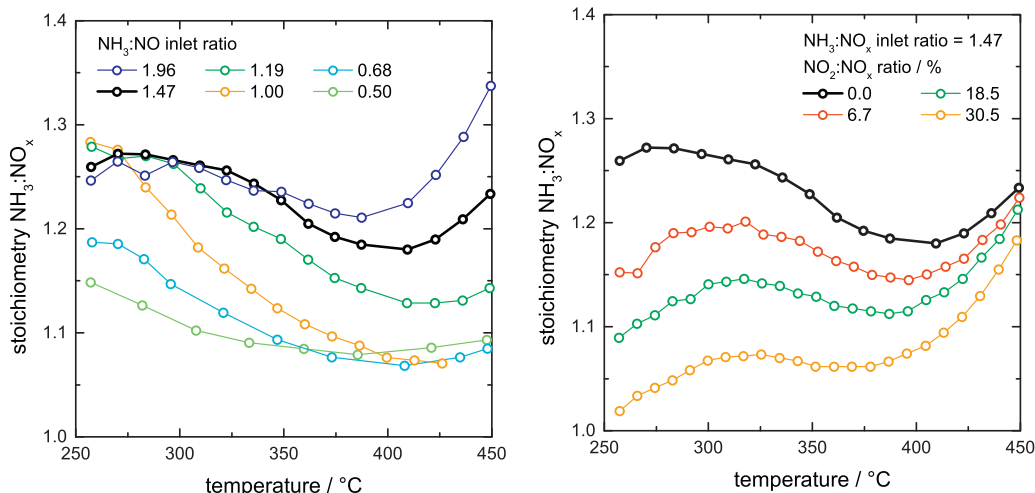
the catalyst. Thus, the equivalent catalyst radius is an approximate measure for the characteristic diffusion length. For the calculation of the effective diffusivities both pore and Knudsen diffusion were taken into account. The kinetic parameters in the expressions for the reaction rates  $r_j$  were determined by the fitting of measured outlet reactor concentrations with the software package Presto-Kinetics. The temperature dependence of the rate constants was described by the Arrhenius equation.

$$k_j = k_{0,j} \exp\left(\frac{-E_{A,j}}{RT}\right) \quad (6)$$

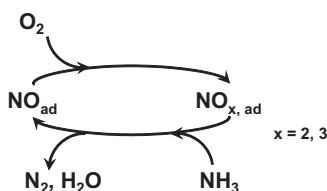
## 3. Results and discussion

### 3.1. Observed stoichiometry of the reaction of NH<sub>3</sub> with nitrogen oxides

Fig. 1 shows an example of the observed NH<sub>3</sub> and NO conversions for an equimolar reactant mixture as a function of temperature. In agreement with earlier studies it can be clearly seen that strong deviations from the 1:1 stoichiometry according



**Fig. 2.** Stoichiometric ratio of converted NH<sub>3</sub> and NO<sub>x</sub> amounts as a function of temperature at different ammonia to nitrogen oxides ratios without NO<sub>2</sub> at reactor inlet (left) and for different NO<sub>2</sub>:NO<sub>x</sub> ratios at an NH<sub>3</sub>:NO<sub>x</sub> ratio of 1.47 (right). 2.5 vol% O<sub>2</sub>, 400 ppm NO<sub>x</sub> and 3100 ppm H<sub>2</sub>O at reactor inlet, catalyst sieve fraction 315–500  $\mu\text{m}$ .



**Fig. 3.** Proposed catalytic redox cycle for the NO assisted  $\text{NH}_3$  oxidation based on the work of Schuler [12,13].

to the reactions (R1) and (R2) occur over the whole temperature range. However, the stoichiometric ratio between the converted amounts of ammonia and NO is also dependent on temperature with significant deviations of up to 30% especially at low temperatures. Further results of the stoichiometric ratio between the converted amounts of ammonia and  $\text{NO}_x$  during SCR measurements are presented in Fig. 2 as a function of temperature. The required stoichiometric ammonia excess ranges from less than 5% to more than 35% depending on the reaction conditions employed.

The left hand side of Fig. 2 shows that the relative ammonia consumption is enhanced by the stoichiometric feed ratio of the reactants. This positive effect of ammonia concentration on the reductant overconsumption is in agreement with Nedyalkova et al. [17]. The ratio of the converted  $\text{NH}_3:\text{NO}_x$  amounts decreases with rising temperature below about  $400^\circ\text{C}$ . This effect cannot be explained by the catalytic oxidation of  $\text{NH}_3$  with  $\text{O}_2$ , as this reaction becomes more and more effective with increasing temperature and is therefore only responsible for the increase of the stoichiometric ratio at higher temperatures, i.e.  $>400^\circ\text{C}$ , as will be shown later.

The variation of the  $\text{NO}_2:\text{NO}_x$  ratio at the reactor inlet also reveals interesting trends (Fig. 2, right). Here it can be seen that the addition of  $\text{NO}_2$  strongly improves the ammonia selectivity at temperatures lower than required for ammonia oxidation with  $\text{O}_2$  (above  $400^\circ\text{C}$ ). Thus, the deviation of the expected 1:1 stoichiometry at low temperatures is evidently enhanced by the presence of high NO concentrations. These findings, which are in agreement with Colombo et al. [16] and Nedyalkova et al. [17], could be explained by a catalytic redox cycle involving NO and adsorbed  $\text{NO}_x$  species (Fig. 3) during which  $\text{NH}_3$  is oxidized by  $\text{O}_2$  [12,13].

### 3.2. Kinetic simulation of $\text{NO}_x$ reduction including $\text{NH}_3$ oxidation in the absence and presence of NO

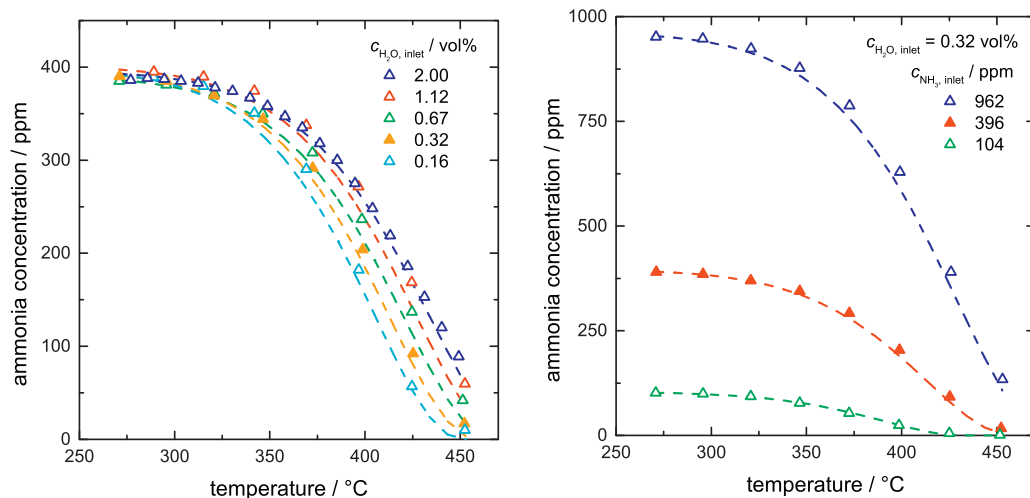
In order to kinetically simulate the overall reaction network those reactions which could be measured independently were investigated first. These were the equilibrium reaction between NO and  $\text{NO}_2$  (R3), the kinetics of which had been described in a previous paper [18], and the catalytic oxidation of  $\text{NH}_3$  in the absence of nitrogen oxides which is described in the following section.

#### 3.2.1. Kinetics of the catalytic oxidation of $\text{NH}_3$

The oxidation of ammonia in the absence of nitrogen oxides was studied in a series of independent measurements over a range of temperatures and reactant concentrations. Due to the relatively low reaction rates, the amount of catalyst had to be increased to 5.97 g which was used without dilution in the reactor. The results can be described with very good accuracy using the kinetic expression given in Table 1 as can be seen from the comparison between calculated and measured results obtained at different water vapor concentrations (Fig. 4, left) and ammonia feed compositions (Fig. 4, right).

**Table 1**  
Concentration dependency  $f(c_i)$  in rate equation

Concentration dependency $f(c_i)$ in rate equation	$k_0$	$E_A/\text{kJ/mol}$	Reaction orders	Adsorption constants
Standard SCR (R1) $\frac{r_{\text{NH}_3}^{r_{\text{O}_2}}}{(c_{\text{NO}} c_{\text{NH}_3} c_{\text{O}_2})} / (1 + K_{\text{NH}_3} c_{\text{NH}_3}^2)$	$9.13 \times 10^{10} \text{ m}^3 \text{ s}^{-1} \text{ kg}_{\text{cat}}^{-1} \text{ mol}^{2.06}$	66.7	$r_{\text{NH}_3} = 1.5$ $r_{\text{O}_2} = 0.56$	$K_{\text{NH}_3} = 4.73 \times 10^7 \text{ m}^6/\text{mol}^2$
Fast SCR (R2) $\frac{r_{\text{NO}_2} c_{\text{NO}} c_{\text{NH}_3}}{(c_{\text{NO}_2}} c_{\text{O}_2}^{n_{\text{O}_2}-0.5})} / (1 + K_{\text{O}_2} c_{\text{O}_2} + K_{\text{H}_2\text{O}} c_{\text{H}_2\text{O}}^{n_{\text{H}_2\text{O}}})$	$5 \times 10^7 \text{ m}^9/\text{kg}_{\text{cat}} \text{ s mol}^2$	36	$r_{\text{O}_2} = 0.75$ $r_{\text{H}_2\text{O}} = 0.5$	$K_{\text{NO}_2} = 27.9 \text{ m}^3/\text{mol}$ $K_{\text{H}_2\text{O}} = 1.98 \text{ m}^{1.5}/\text{mol}^{0.5}$ $K_c = c_{\text{NO}_2}^2 / (c_{\text{NO}}^2 c_{\text{O}_2})$ $K_{\text{H}_2\text{O}} = 19.1 \text{ m}^{0.9}/\text{mol}^{0.3}$
NO oxidation [18] (R3) $\frac{r_{\text{NO}_2}}{(c_{\text{NO}_2}} c_{\text{O}_2}^{n_{\text{O}_2}-0.5})} / \sqrt{K_c} / (1 + K_{\text{O}_2} c_{\text{O}_2} + K_{\text{H}_2\text{O}} c_{\text{H}_2\text{O}}^{n_{\text{H}_2\text{O}}})$	$10.35 \text{ m}^{5.25}/\text{kg}_{\text{cat}} \text{ s mol}^{0.75}$	31	$r_{\text{NH}_3} = 0.6$ $r_{\text{O}_2} = 0.3$ $r_{\text{H}_2\text{O}} = 0.3$	$K_{\text{NH}_3} = 1.11 \times 10^4 \text{ m}^6/\text{mol}^2$
$\text{NH}_3$ oxidation with $\text{O}_2$ (R4) $\frac{r_{\text{NH}_3}^{r_{\text{O}_2}}}{(c_{\text{NH}_3}} c_{\text{O}_2})} / (1 + K_{\text{H}_2\text{O}} c_{\text{H}_2\text{O}}^{n_{\text{H}_2\text{O}}})$	$6.83 \times 10^5 \text{ mol}^{0.1} \text{ m}^{2.7}/\text{kg}_{\text{cat}} \text{ s}$	96.3	$r_{\text{NH}_3} = 0.98$ $r_{\text{O}_2} = 1.03$	
NO assisted $\text{NH}_3$ oxidation (R4) $\frac{r_{\text{NO}}^{r_{\text{O}_2}} c_{\text{NH}_3}}{(c_{\text{NO}} c_{\text{O}_2} c_{\text{NH}_3})} / (1 + K_{\text{NH}_3} c_{\text{NH}_3}^2)$	$2.58 \times 10^4 \text{ m}^{9.03}/\text{kg}_{\text{cat}} \text{ s mol}^{2.01}$	48		

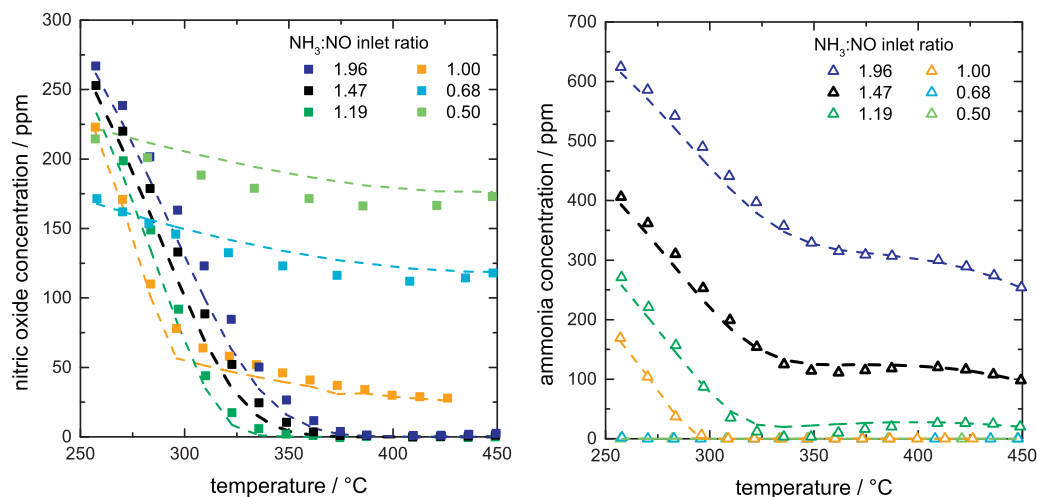


**Fig. 4.** Measured and calculated  $\text{NH}_3$  outlet concentrations as a function of temperature for different water (left) and ammonia (right) concentrations at reactor inlet. 2.5 vol%  $\text{O}_2$ , 0 ppm  $\text{NO}_x$  at reactor inlet, catalyst mass 5.97 g, catalyst sieve fraction 315–500  $\mu\text{m}$ . Symbols: measurements, broken lines: simulations.

### 3.2.2. Kinetics of the NO assisted selective catalytic oxidation of $\text{NH}_3$

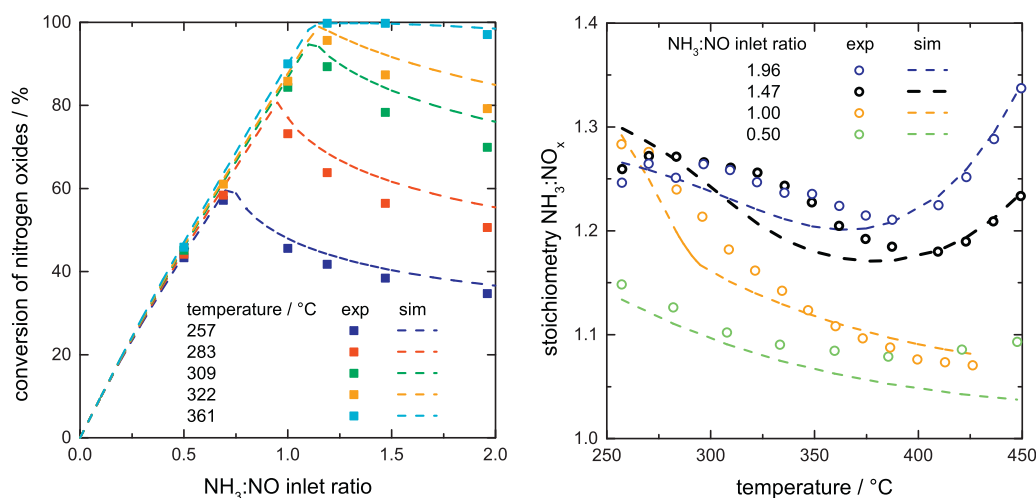
For analysis of the measured data regarding the ammonia oxidation in the presence of nitrogen oxides, all reactions (R1) to (R4) had to be considered simultaneously. For this purpose the kinetics for NO and  $\text{NH}_3$  oxidation were complemented by kinetic descriptions of the  $\text{NO}_x$  reduction. For the *standard* SCR, a Langmuir–Hinshelwood-type rate equation was used (Table 1). In agreement with the literature [1,4,11–15], the *fast* SCR was assumed to be first order with respect to the concentrations of NO,  $\text{NO}_2$  and  $\text{NH}_3$ . The activation energy for the *fast* SCR was used from Schuler [13] and the frequency factor was determined during the overall parameter fitting. For the NO assisted oxidation of  $\text{NH}_3$  it was assumed that this reaction has the same stoichiometry as reaction (R4) and that its reaction rate is proportional to the NO concentration. The underlying physical basis can be derived from the above postulated catalytic redox cycle (Fig. 3), that leads to a concurrent enhancement of ammonia oxidation by  $\text{O}_2$ . Hence it is assumed that the surface concentration of the adsorbed NO species is proportional to the NO gas phase concentration. All rate equations and the kinetic parameters obtained in the concluding parameter fitting for the overall reaction network are summarized in Table 1.

Fig. 5 shows the comparison between measured and calculated reactor outlet concentrations of NO (left) and  $\text{NH}_3$  (right) as a function of temperature for a series of measurements where  $\text{NO}_x$  was fed as NO only. It can be seen that the measured data are correctly described in a range of  $\text{NH}_3$ :NO feed ratios between 0.5 and about 2. The left hand side of Fig. 5 reveals that the achievable NO conversion remains significantly below 100% even at high temperatures for  $\text{NH}_3$ :NO feed ratios  $\leq 1$ . For stoichiometric feed ( $\text{NH}_3$ :NO = 1, orange symbols), the NO outlet concentration approaches some 30 ppm for high temperatures while  $\text{NH}_3$  is already completely consumed at around 300 °C. This shows again to which extent ammonia is excessively consumed during SCR on the iron zeolite catalyst. For  $\text{NH}_3$ :NO feed ratios exceeding unity, NO conversion always approaches 100%. The required temperature for full NO conversion increases with rising ammonia concentration which can be explained by the inhibiting effect of  $\text{NH}_3$  on the rate of the *standard* SCR reaction. An interesting phenomenon can be seen in the right hand diagram of Fig. 5 for an  $\text{NH}_3$ :NO feed ratio of 1.19. With rising temperature, ammonia reaches almost complete conversion at around 330 °C, but at even higher temperatures, the  $\text{NH}_3$  outlet concentration increases again. This phenomenon is caused by the different distribution of NO concentrations in the integral reactor during these measurements and will be interpreted later.



**Fig. 5.** Measured and calculated outlet concentrations of NO (left) and  $\text{NH}_3$  (right) as a function of temperature for different ammonia to nitric oxide ratios at reactor inlet. 2.5 vol%  $\text{O}_2$ , 400 ppm NO and 3100 ppm  $\text{H}_2\text{O}$  at reactor inlet, catalyst sieve fraction 315–500  $\mu\text{m}$ . Symbols: measurements, broken lines: simulations.





**Fig. 6.** Measured and calculated  $\text{NO}_x$  conversions (left) and stoichiometric ratios (right) as a function of the  $\text{NH}_3:\text{NO}$  ratio at reactor inlet at different temperatures. 2.5 vol%  $\text{O}_2$ , 400 ppm NO, and 3100 ppm  $\text{H}_2\text{O}$  at reactor inlet. Symbols: measurements, broken lines: simulations.

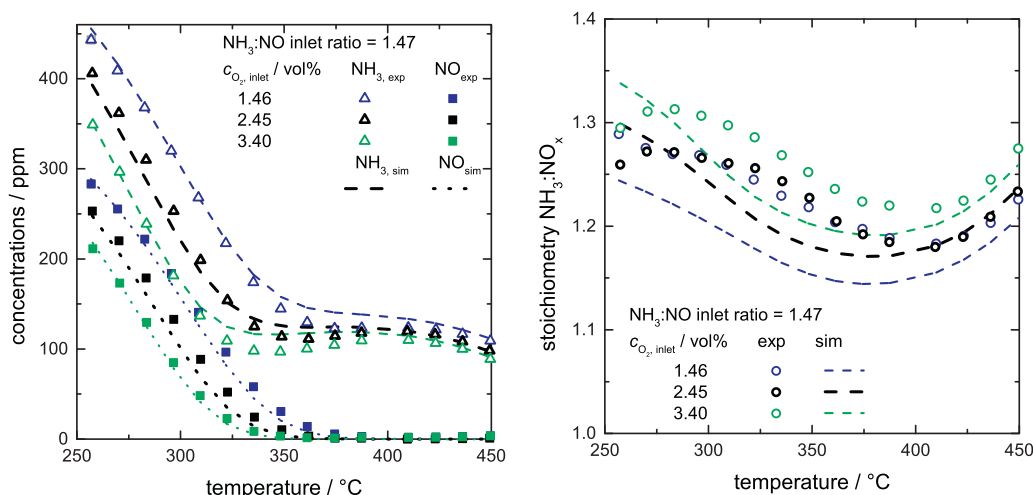
Fig. 6 depicts selected data of the series of measurements shown in Fig. 5 in a different form. In the left hand diagram, the achieved  $\text{NO}_x$  conversion is plotted as a function of the  $\text{NH}_3:\text{NO}$  ratio at reactor inlet. Here, the deviation from the 1:1 stoichiometry can be recognized by a decreased slope of the curves before reaching the maximum  $\text{NO}_x$  conversion. The right hand diagram of Fig. 6 reveals a relatively good agreement between measured and calculated stoichiometric ratios of the converted  $\text{NH}_3$  and NO amounts.

Comparison of the activation energies determined for the different reactions occurring allows the temperature dependency of the stoichiometric deviations during  $\text{NH}_3$  conversion to be explained. Since the NO assisted ammonia oxidation has a low activation energy of 48 kJ/mol, the relative contribution of this reaction path is quite high at low reaction temperatures. With rising temperature, the rate of the *standard* SCR with an activation energy of approx. 67 kJ/mol is accelerated more strongly than the NO assisted  $\text{NH}_3$  oxidation, and the stoichiometric ammonia excess decreases. At even higher temperatures, however, the ammonia oxidation by  $\text{O}_2$  with the highest activation energy of around 96 kJ/mol gives again rise to larger deviations from the 1:1 stoichiometry.

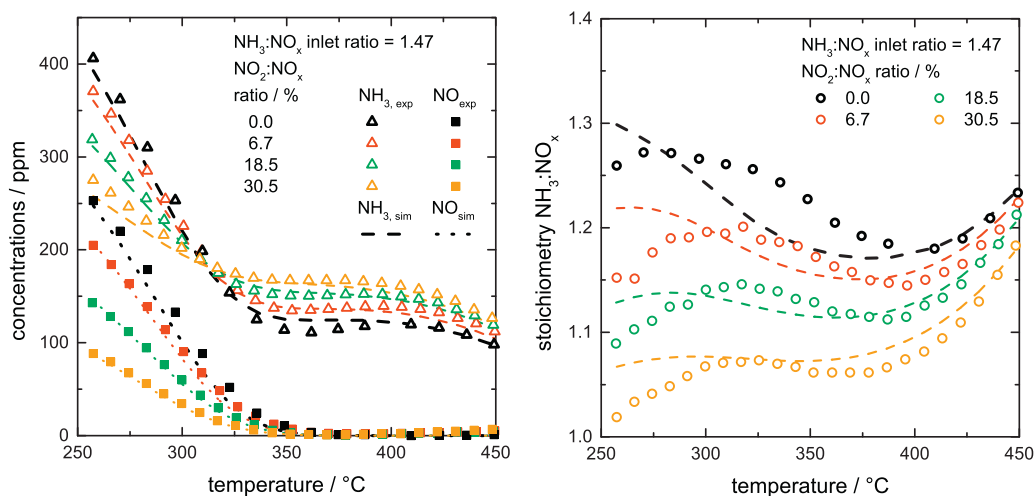
Results depicted in Fig. 7 reveal that the variation of the oxygen feed concentration can also be successfully modeled with the kinetic equations developed. One can see from the right hand diagram of Fig. 7 that the required ammonia excess increases in the

presence of higher  $\text{O}_2$  concentrations. While the temperature trend and the minima of the ammonia excess at a temperature of around 400 °C are correctly captured by the kinetic model, the description of the stoichiometric ratio (Fig. 7, right) succeeded in a merely qualitative manner. Regarding the absolute exactness it has to be taken into account that the chosen representation of the data is extremely sensitive to small differences between measured and calculated results.

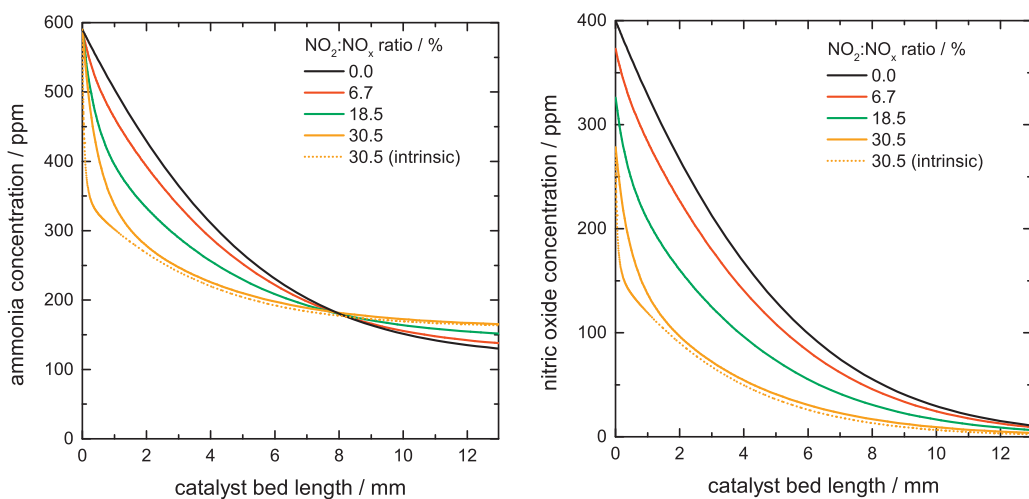
Further measurements with different mixtures of NO and  $\text{NO}_2$  at the reactor inlet were also carried out. The results in Fig. 8 for an  $\text{NH}_3:\text{NO}_x$  ratio of 1.47 at the reactor inlet show that the addition of  $\text{NO}_2$  at a constant total  $\text{NO}_x$  concentration (400 ppm) accelerates the conversion of  $\text{NH}_3$  only at temperatures below about 320 °C. This can be easily explained by the enhancing effect of  $\text{NO}_2$  through the *fast* SCR. In all cases, no  $\text{NO}_2$  could be detected at reactor outlet. However, the remaining ammonia concentration at 350 to 400 °C, where the nitrogen oxides are always completely consumed, is significantly higher for gas mixtures containing  $\text{NO}_2$  than in the case of pure NO in the feed. This is due to the enhancing effect of NO on the oxidation of ammonia whereas in the presence of  $\text{NO}_2$ , NO apparently reacts very fast and thus selectively with  $\text{NH}_3$  and  $\text{NO}_2$  according to reaction (R2) and leads to an improvement of the required stoichiometric excess of the reducing agent (Fig. 8, right). However, it cannot be derived from our measurements if the



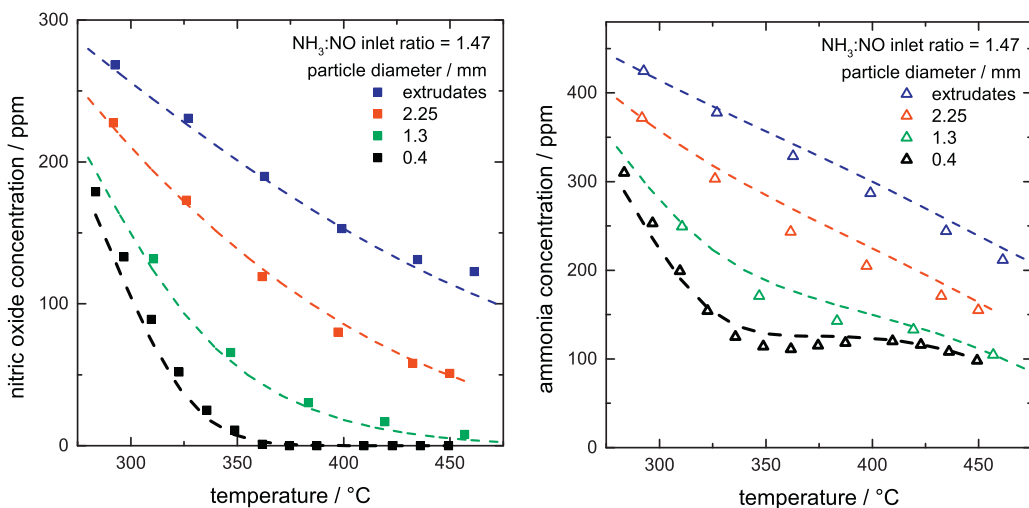
**Fig. 7.** Measured and calculated outlet concentrations of NO and  $\text{NH}_3$  (left) and stoichiometric ratio (right) as a function of temperature for different oxygen concentrations at reactor inlet. 590 ppm  $\text{NH}_3$ , 400 ppm NO and 3100 ppm  $\text{H}_2\text{O}$  at reactor inlet, catalyst sieve fraction 315–500  $\mu\text{m}$ . Symbols: measurements, broken lines: simulations.



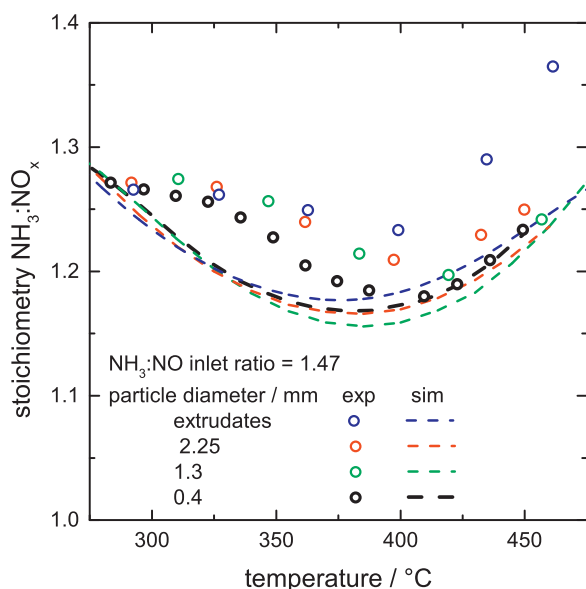
**Fig. 8.** Measured and calculated outlet concentrations of NO and NH<sub>3</sub> as a function of temperature for different NO<sub>2</sub>:NO<sub>x</sub> ratios at reactor inlet. 2.5 vol% O<sub>2</sub>, 590 ppm NH<sub>3</sub>, 400 ppm NO<sub>x</sub> and 3100 ppm H<sub>2</sub>O at reactor inlet, catalyst sieve fraction 315–500 μm. Symbols: measurements, broken lines: simulations.



**Fig. 9.** Calculated concentrations of NH<sub>3</sub> (left) and NO (right) as a function of catalyst bed length for different NO<sub>2</sub>:NO<sub>x</sub> ratios at reactor inlet. Particle diameter 400 μm, reactor temperature 343 °C, 2.5 vol% O<sub>2</sub>, 400 ppm NO<sub>x</sub>, 590 ppm NH<sub>3</sub> and 3200 ppm H<sub>2</sub>O at reactor inlet.



**Fig. 10.** Measured and calculated outlet concentrations of NO (left) and NH<sub>3</sub> (right) as a function of temperature for different catalyst particle sizes. 2.5 vol% O<sub>2</sub>, 400 ppm NO, 590 ppm NH<sub>3</sub> and 3100 ppm H<sub>2</sub>O at reactor inlet. Symbols: measurements, broken lines: simulations.



**Fig. 11.** Measured and calculated stoichiometric  $\text{NH}_3:\text{NO}_x$  ratios as a function of temperature for different catalyst particle sizes. 2.5 vol%  $\text{O}_2$ , 400 ppm  $\text{NO}$ , 590 ppm  $\text{NH}_3$  and 3100 ppm  $\text{H}_2\text{O}$  at reactor inlet. Symbols: measurements, broken lines: simulations.

$\text{NH}_3$  oxidation is enhanced in the presence of  $\text{NO}_2$  since only gas mixtures with  $\text{NO}_2:\text{NO}_x$  ratios lower than 50% were used. In order to achieve a better understanding of the observations, the simulated  $\text{NH}_3$  and  $\text{NO}$  concentrations as a function of reactor length are depicted in Fig. 9 for different  $\text{NO}_2:\text{NO}_x$  ratios at a reactor temperature of 343 °C and feed concentrations of 400 ppm  $\text{NO}_x$  and 590 ppm  $\text{NH}_3$ , respectively. The predicted ammonia concentration in the inlet zone of the reactor strongly decreases upon addition of  $\text{NO}_2$ . However, the ammonia concentration curves intersect each other at a catalyst bed length of about 8 mm while at reactor outlet the sequence of ammonia concentrations is inverted with higher values occurring for  $\text{NO}_2$ -containing feeds. This can be explained by the corresponding higher average  $\text{NO}$  concentration levels in the reactor (Fig. 9, right) giving rise to larger amounts of ammonia being oxidized. In a similar manner, the peculiarities of the  $\text{NH}_3$  outlet concentration versus temperature during certain measurements depicted in Fig. 5 can be understood. Specifically, the fact that the  $\text{NH}_3$  outlet concentration during the measurement with

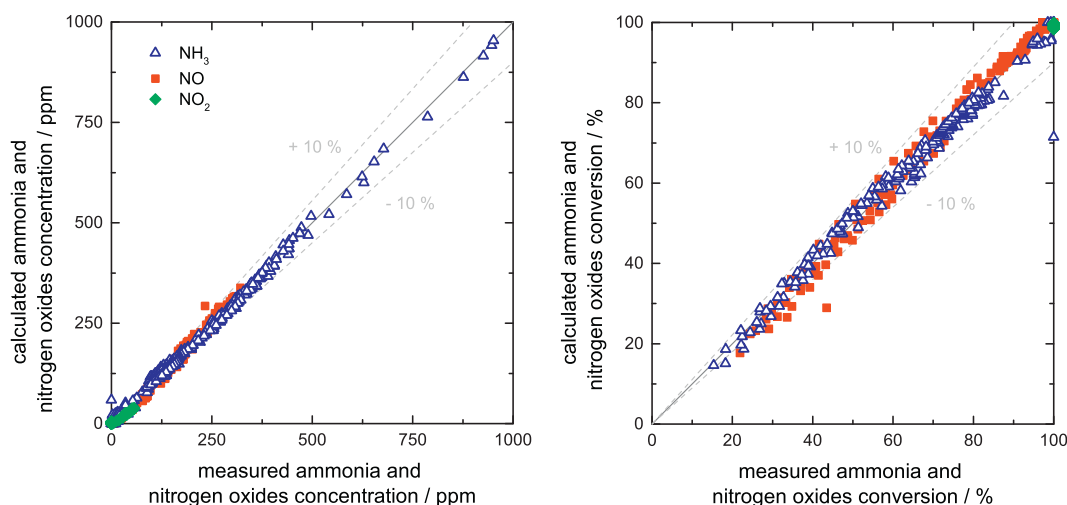
an  $\text{NH}_3:\text{NO}$  inlet ratio of 1.19 (green symbols) reaches almost zero at around 350 °C and then again increases at higher temperatures, is also caused by the corresponding different average  $\text{NO}$  levels in the reactor.

The diagrams of Fig. 9 also show comparisons between calculated values obtained with the full reactor model and with the intrinsic kinetics in the absence of any mass transfer resistances. Differences can only be seen directly at the reactor inlet, where  $\text{NO}_2$  is still present and the extremely rapid fast SCR (R2) occurs.

### 3.3. Influence of catalyst particle diameter

The overall model developed, including mass transport effects, was finally validated with different catalyst sieve fractions including commercial catalyst extrudates. The comparison of measured and calculated  $\text{NO}$  and  $\text{NH}_3$  concentrations at the reactor outlet depicted in Fig. 10 reveals that the influence of film and pore diffusion on the overall reaction rates can be described with good accuracy. The performance of commercial extrudates is drastically diminished compared to the smallest sieve fraction (average diameter 0.4 mm) with which the intrinsic chemical kinetics could be measured over the whole range of conditions studied. While in this case complete  $\text{NO}$  consumption is always obtained above 350 °C, the extrudates only allow for  $\text{NO}$  conversions of about 50% (350 °C) to around 75% (450 °C). This shows that small catalyst diffusion lengths (e.g. in coated honeycomb monolith structures) are beneficial for achieving a high utilization of the catalytic material. On the other hand, the simulation reveals that mass transfer resistances have little influence on the required stoichiometric ammonia amount (see Fig. 11). However, the differences resulting from the variation of particle size are considerably smaller than the scatter in the experimental data points.

Overall, the kinetics developed allow the rates of  $\text{NH}_3$  and nitrogen oxides conversions to be described with very good accuracy as shown in the parity plots for reactant concentrations (Fig. 12, left) and conversions (Fig. 12, right). The mean deviation between measured and calculated concentrations amounts to 4.5 ppm, which is equivalent to a mean relative error of 8.0% (assuming a detection limit of 5 ppm). Regarding the conversions, we obtained an absolute deviation of only 1.1%. This corresponds to an average relative error of 2.3% (measurements without  $\text{NO}_2$  at reactor inlet not taken into account). The used set of data (overall 669) also included the independent measurements for the variation of the catalyst particle diameter.



**Fig. 12.** Parity plot for all measured  $\text{NH}_3$  and nitrogen oxides concentrations at reactor outlet (left) as well as for  $\text{NH}_3$  and nitrogen oxides conversions (right).



#### 4. Conclusions

Steady-state measurements of the reduction of nitrogen oxides with ammonia in the presence of oxygen were carried out in an integral reactor over a commercial iron zeolite catalyst at different temperatures, concentrations and catalyst particle sizes. The kinetics of the catalytic oxidation of  $\text{NH}_3$  with  $\text{O}_2$  were determined in separate measurements in the absence of nitrogen oxides. Kinetic analysis of the measured data with global Langmuir–Hinshelwood-type rate equations revealed that the observed deviations from the expected 1:1 stoichiometry of the  $\text{NH}_3$ –NO reaction cannot be explained only by the parallel reaction of ammonia with oxygen, which is mainly responsible for the increased ammonia oxidation above reaction temperatures of around 400 °C. For successful description of the measurements at lower temperature, a second kinetic expression for the NO assisted ammonia oxidation had to be introduced in which the rate is not only proportional to the  $\text{NH}_3$  and  $\text{O}_2$  concentrations, but also to the NO concentration. These findings are in agreement with Colombo et al. [16] and Nedyalkova et al. [17] and support earlier suggestions by Schuler et al. [12,13] revealing that NO forms a surface species which passes through a redox cycle and consumes  $\text{NH}_3$  for reduction and  $\text{O}_2$  for oxidation. It could be furthermore shown that the *fast* SCR is very selective and does not lead to additional ammonia oxidation. Measurements with different catalyst particle sizes revealed that mass transfer resistances strongly affect the overall reaction kinetics, especially for the catalyst extrudates of commercial size. In that case, ammonia oxidation is even more pronounced than under reaction conditions where intrinsic chemical kinetics prevail. The kinetic model developed allows, for the first time, to calculate with good accuracy the amount of ammonia required for the selective catalytic reduction of NO and  $\text{NO}_2$  over iron zeolites over a broad range of reaction conditions.

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